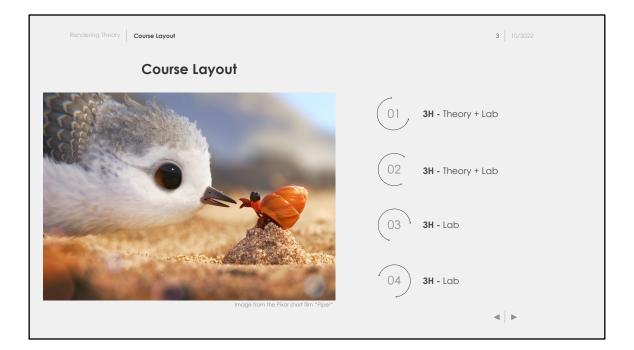


Not going to talk too much about me, but I have spent most of my time on rendering on my day job and on my spare time.

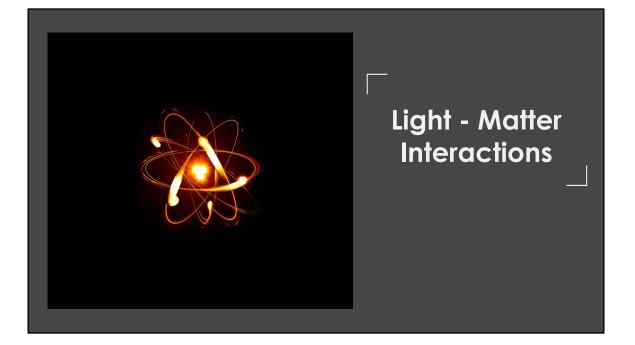
The goal of this course is not only to teach you rendering, but also to make you love it as much as I do :)

From Sketchfab (as an intern) to Wonderland GmbH, I have always been working on real time rendering.

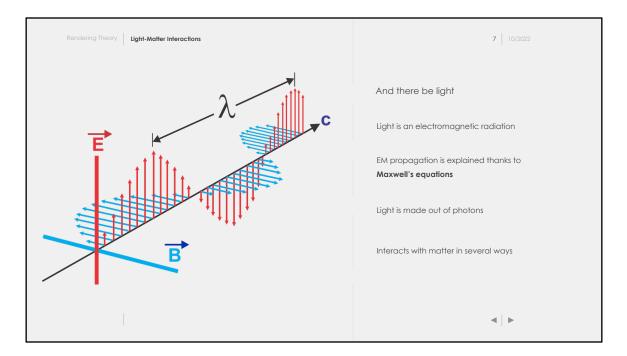
As you can see, there are a lot of possibilities even in different / unexpected fields, such as medical imaging.





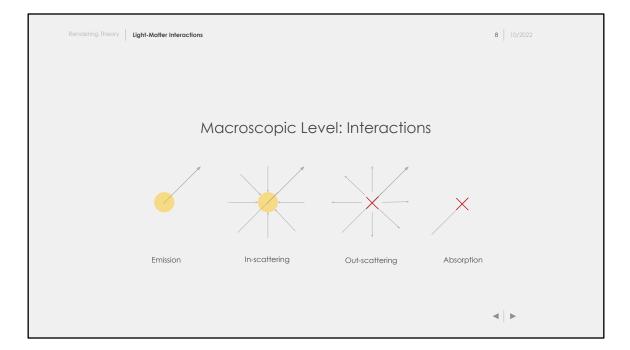


Rendering Theory Light-Matter Interactions	6   10/2022
Disclaimer	
I am not a physicist, and <b>Quantum Mechanics</b> is a really complex topic. This section aims at giving you some insight that will help you understand better how our mathematical models are derived.	
It's also a rabbit hole, the deeper you question the nature around you, the more questions will start popping in your head.	
	< ►



If you recall your lessons from High School, light is made out of photons. A photon can be thought as a particle or as a wave. This is called the **Wave-particle** duality.

The wave nature of light can be studied via Maxwell's equation, that help us understand how lights propagate throughout a medium.



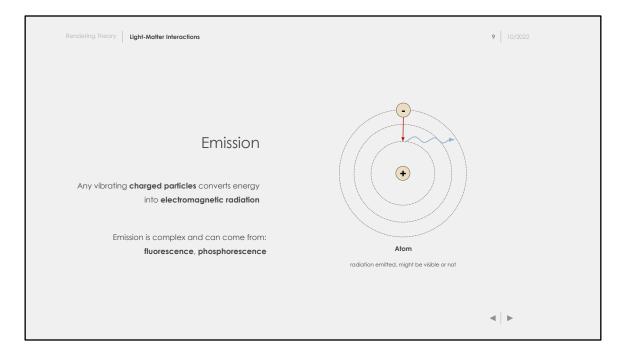
When light interacts with matter, it undergoes interactions that depends on:

- The interface between the two mediums
- The light beam direction
- The wave polarization (out of the scope of this course)

At a macroscopic levels, those interactions are often sorted into three or four categories:

- Emission: light is created (transfer of energy occurs)
- In-Scattering: light arrives at a particle
- Out-Scattering: light leaves a particle
- Absorption: light is absorbed by matter and an energy transfer occurs (e.g: heat)

This is just an overview, and we will go over what happens at the atomic level on the next slides.

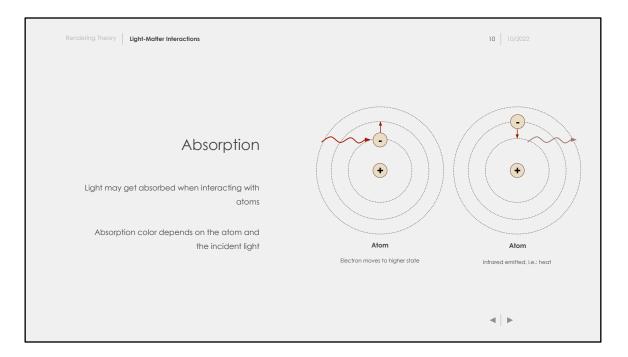


Atoms are made out of electrons outside of their nucleus. It's common to depict electrons as orbiting around their nucleus like here, using the Niels Bohr model.

When an electron is in a higher level of energy, it will try to reach its original state releasing electromagnetic radiation. The wavelength of the emitted radiation depends on the state the electron was previously in.

Now the question might be: how do we get an electron to a higher level of energy? Everything above absolute zero radiates light. There are a lot of conversion that can happen, like thermal energy into electromagnetic energy.

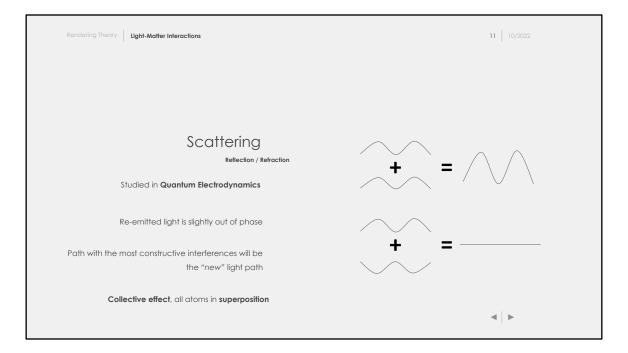
Just a side note here, the **Bohr** model isn't fully accurate. Electrons aren't really particles in ring like that. In reality, electrons occupy **atomic orbitals**, which are region of **probabilistic location**.



Electromagnetic waves interact with electrons if the incident energy can make the electron reach a higher state of energy. When going to a higher state, the incident energy is absorbed.

A small amount of time later, the electron goes back to its initial energy state and radiation is emitted. The wavelength of the emitted radiation depends on the state the electron was previously in.

In some materials, atoms/molecules are physically close to each other (dense), and absorption is the result of conversion from electromagnetic energy into thermal energy (vibrations).



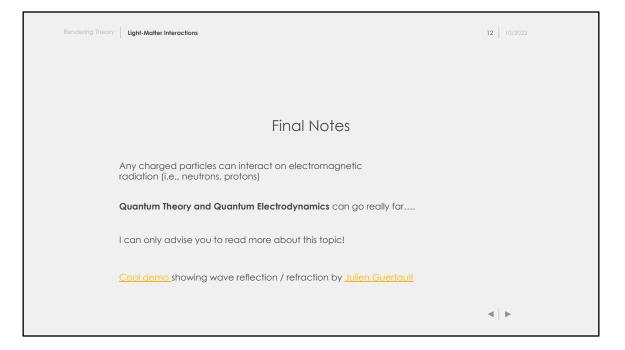
**QM** is inherently probabilistic, and it's not possible to follow the path of a single photon. However, if we mix **QM** and classical physics, we can obtain an intuition of what's happening.

Atoms will absorb photons and re-emits them like we saw on the previous slide. However, you can think of the atom as a punctual light source emitting in every directions. The emitted radiation phase is dependent on the incoming beam.

When photons interact at the intersection between two mediums, the light reflection/refraction path will be the ones with the most constructive interferences. At the opposite, the incoming wave will be the path where most of the destructive interferences occurs.

I want to stress out just one thing: in reality, changing speed is a collective effect and not the result of a **single atom** interaction. Photons actually scatter from **all** atom **simultaneously** (crazy, right?).

At a higher level, **Maxwell's equations** help us derive the **Fresnel** equations that are used to compute the ratio of reflected light over refracted light. We will talk about later in the Physically Based Rendering course.

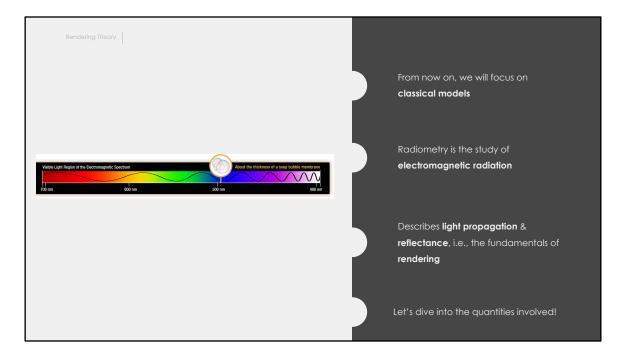


Don't forget that the Bohr model we looked at is a more simple representation of what occurs.

**Quantum Theory and Quantum Electrodynamics** help explain some effects that can't be explained using classical models.

For instance, it's not possible to study the path of a single elementary particle. A photon actually doesn't interact with a single electron at a time, but with all of them **simultaneously**... Crazy, isn't it?



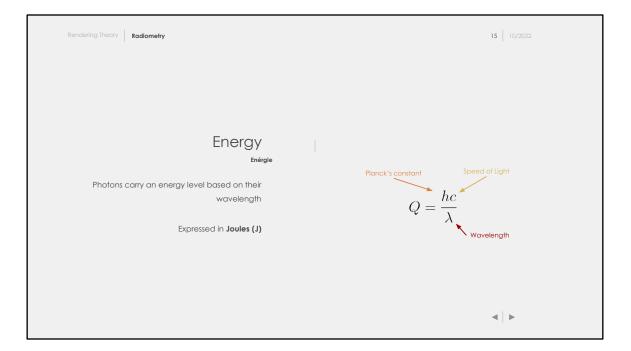


We have had a good look at some of the models that help explain what happens to electromagnetic radiation at the atomic level.

However, for rendering purposes, we will use **higher level models**. Our goal is to render an image, and for that we have to study energy exchange at a high level.

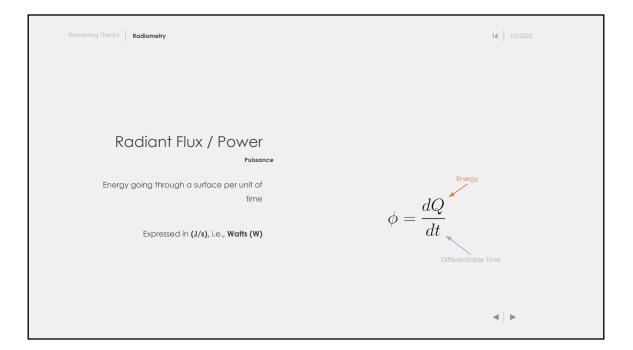
Radiometry can basically be thought as the field of study of electromagnetic radiations and their propagation. It will give us the necessary tools to work our way into the Rendering Equation. From now on, we will not need to dive into quantum physics and we will keep a much simpler vision: light is made out of photons that travel on a straight path.

Let's build this equation part by part together!



Radiometry is interested into measuring electromagnetic radiation. Electromagnetic radiations are composed of photons which carry **energy**.

You might remember the equation above from high school, used to compute the total energy of a photon.



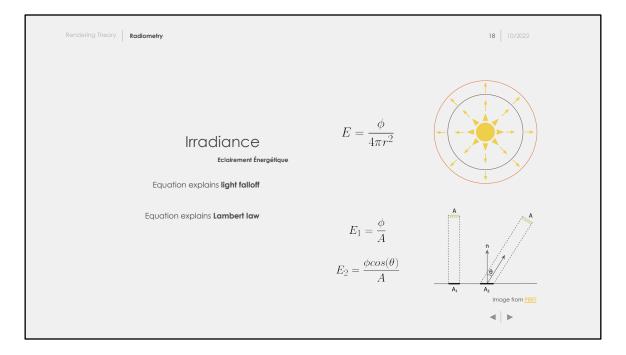
We are often interested in the flux, i.e., the energy per unit of time. In reality, we will often assume we are in a **steady state** for simplicity.

Rendering Theory Radiometry	17   10/2022
Irradiance Eclairement Énergétique	Power
Radiant Flux received per <b>unit area</b>	$E(p) = \frac{d\phi(p)}{dA}$
Irradiance = incoming,	Finite Surface Area
Radiant Exitance = outgoing	
Expressed in <b>(W/m2)</b>	
	< ►

Irradiance is defined as the radiant flux received per surface of area A. This is one of the most useful quantities we often use in rendering. We are often interested in knowing how much light is reaching a point in the hemisphere oriented around the normal of the surface of interest.

There is a distinction between:

- Incoming radiant flux per unit area is called Irradiance
- Outgoing radiant flux per unit area is called Radiant Exitance



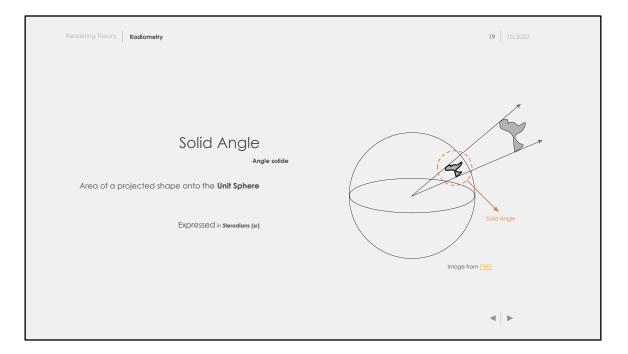
As stated in PBRT book, the irradiance equation makes us realize two things:

- For a perfect point light, the energy falls off with the squared distance from the light origin
- Helps us understand the Lambert Cosine Law

Shining a light with an angle at a surface will create a larger projected area (A2 on the drawing). A larger

area implies a smaller Irradiance. It also makes sense intuitively, the flux is then dispatched on a larger

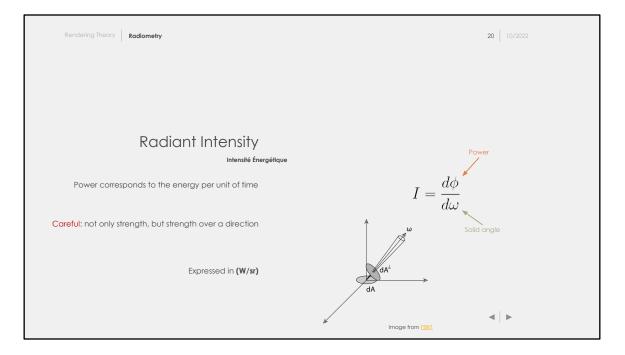
surface and each "point" receives less power and so less energy.



We are often interested into bringing directionality when talking about radiometry.

Solid angles describes the projected area of an object onto the unity sphere. You can imagine for instance being an observer at the center of the sphere, looking at the projected silhouette of the object on the edges of the sphere.

You might not exactly understand yet why we are talking about that, but we will soon make the connection.



In physics, it's defined as the radiant flux (the power) per unit area. In the case of Radiometry however, the intensity is defined as the **power per unit solid angle**.

Be careful here, intensity isn't exactly synonymous to **'strength'** or **'magnitude'**. It's the strength over a given direction and area.

When taking the intensity emitted by a light source, the solid angle corresponds to the surface into which the flux is emitted. When computing the received intensity at a point, the solid angle corresponds to the area subtended by the source **as seen** from the point.

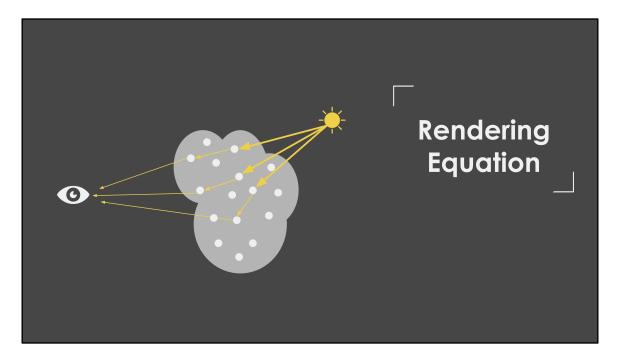
With intensity, it's possible to derive the strength and direction of light. Because we care mostly about direction, we will in general the limit of a differential cone, i.e., infinitesimally small solid angle.

Rendering Theory Radiometry	21   10/2022
Radiance Luminance Energétique	
Radiant Intensity leaving an area A, over solid angle omega	$L(p,\omega)=\frac{dE_{\omega}(p)}{d\omega}=\frac{d\phi(p)}{d_{\omega}dA^{\perp}}$
This is <b>The Quantity</b> to remember	μ μ μ
Combination of all other quantities	
Expressed in <b>(W.sr<sup>-1</sup>.m<sup>-2</sup>)</b>	dA

Radiance allows to express irradiance or radiant exitance in terms of solid angle, bringing **directionality** into our equations!

Remember that our final goal is to perform rendering, which basically consists in computing radiance coming from viewing direction onto a sensor (e.g., eye, camera). We are interested in the radiance coming into the camera, for every pixel direction.

Radiance is also a combination of all the previous quantity we have seen, and can be used to get back to other quantity by using integration.



We have talked about light-matter interactions as well as Radiometry. Now we need to come up with

an equation that can represents those interactions and gives us information about the spectral

distribution of light as it undergoes reflection / refraction.

Fortunately for us, a lot of smart people spent time figuring it out, and came up with an equation.

Rendering Theory Introduction		23   10/2022
	Disclaimer The rest of the course will assume that	
Light travels in vacuum	We deal only with opaque surfaces	Interactions occur at object surface
		< ►

Just a little disclaimer before continuing. This entire course is based on a few assumptions:

- Light travels in vacuum (No gas interaction)
- We will only cover opaque surfaces, for simplicity
- Interactions occur only at objects surfaces

All those assumptions will help us simplify our equations and thus our rendering algorithms. With this assumptions, you will already see that solving the rendering equation isn't an easy task, especially in real time! 😌

Rendering Theory	Introduction		24   10/2022
		Neglected Effects	
1	No transmission		
2	No Subsurface Scattering		There are ways to simulate some of those effects. However, it's out of scope for this lesson.
3	No Phosphorescence		Additional links will be given for readers that want to go further!
4	No Fluorescence		
			< ►

Rendering Theory Rendering Equation	25   10/2022
Definition Rendering Equation	
We are interested in computing the radiance reaching the viewer	$L_o(p,\omega_o) = \int_{\Omega} \underbrace{f_r(p,\omega_o,\omega_i)}_{\swarrow} L_i(p,\omega_i) n \cdot \omega_i d\omega_i$
This equation will allow us to compute it!	BRDF
Recursive	
	◄   ►

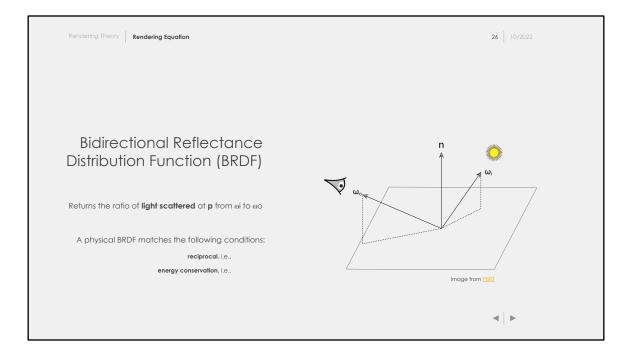
The above equation gives the radiance leaving in the direction  $\omega o$ , due to illumination at point **p** from all directions in the oriented in the hemisphere aligned to the surface normal.

As you can see, this equation is **recursive** and depends on incoming radiance from all over the hemisphere oriented around the surface normal. This is why rendering photorealistic images is a computational heavy problem: you need to compute incoming light from many directions **recursively** to determine the final color of a pixel.

We will first break down together this equation, and see how it can be retrieved. There exist several mathematical tools to describe how light is reflected and transmitted. However,

as mentioned at the beginning of this course, we will only focus on opaque surfaces with interactions

occuring at the object surfaces.



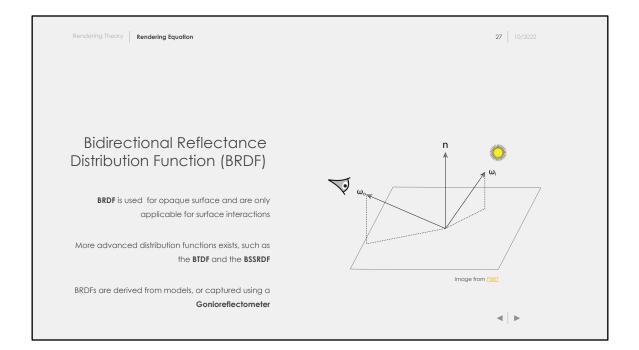
The **BRDF** is used to weight incoming radiance over the hemisphere. It describes how much light from a direction  $\omega$ i gets reflected in direction  $\omega$ o. Stated differently, the BRDF helps you know how much of the light coming from a particular direction will contribute to the result direction ( $\omega$ o).

ωo is often called the **"view" direction**, and ωi the **"light" direction**.

The function is driven by the material properties and helps define its appearance.

It's really important to remember the two conditions listed above. A BRDF must follow those rules in order to be physical. The energy conservation rule is especially important because energy is always transferred between systems.

You may also wish to have a non-physical BRDF to perform some non-realistic rendering, but that's another story.

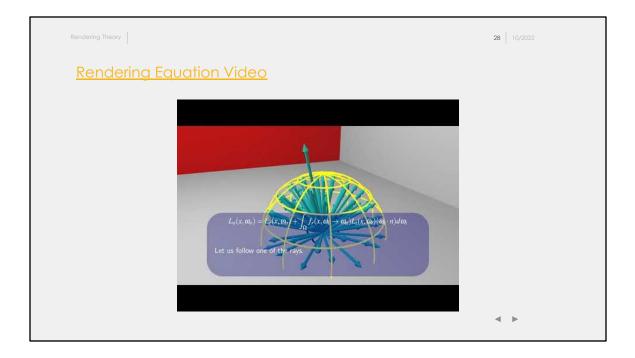


In reality, light penetrates an object and interacts with particles. Lights will scatters inside the material and gets absorbed or eventually leave the material. *"Remaining"* wavelengths are what gives objects their colors.

This is why there are other formalism, such as the:

- **BTDF**: Describes the behavior of transmission
- **BSSRDF**: Describes the subsurface behavior of light. Light enters at point A but might leave at point B

My goal here is just to present other mathematical tools that can help us describe more complex behaviors that exist in nature. We mentioned already that we only care about a single point of interaction at the object surface. So for this entire course, we will **always** focus on **BRDFs** and nothing else.



Rendering Theory Rendering Equation	<b>29</b> 10/2022
Final Notes	
Rendering equation uses all quantities we have seen	
The rendering equation is what we solve when generating 3D images	
A good explanation of how to derive the equation is available in <u>PBRT</u>	
	◄   ►



Rendering Theory	31   10/2022
References	
[Hébert15], M. Hébert, R.D. Hersch, P. Emmel, Fundamentals of Optics and Radiometry for Color Reproduction	
[Kajiya86], J. T. Kajiya, The Rendering Equation	
[Pharr18], M. Pharr, W. Jokob, and G. HUmphreys, Physically Based Rendering: From Theory to Implementation	
[Gui], R. Gui, M. Agopian, Physically Based Rendering in Filament	
[Glassner95], A. S. Glassner, Principles of Digital Image Synthesis	
	< ►

